Situated Actions and Cognition

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Abstract

The paper addresses the concept of cognition starting from the role of a sensor basis in the design of robots. The field of robotics forces the discussion to be *pragmatic* which is considered to be advantageous. In addition, we introduce the notion of *cognitive basis* in order to discuss the cognitive abilities of an artificial creature. As cognition cannot be fully separated from action and acting, we present finally the notion of *motor-schema basis*. This basis involves actions and acting as integral parts of cognition.

1 Introduction

Discussions about robotics/artificial life as well as about (human) perception/mind show the prominence of the concept of *cognition*. In general, the process of cognition relies on many - in a certain sense autonomous - *perceptual mechanisms*. Researchers in the fields of robotics and artificial life tend to adopt a point of view about perception and "mental activities" which stresses the *action-driving* aspect. Such a viewpoint conflicts with what is called *symbolic AI*. Symbolic AI is concerned with "high-level" cognition which is usually equated with (formal) symbol-structure manipulation. This outlook ignores any necessary connection between perception and action. Our purpose is to provide a more action-driven perspective on cognition and intentionality. We take our starting point in the field of robotics as it enforces a rather pragmatic approach to the action-driving aspect of cognitive creatures. One has to take the *design stance*, and is not so much bothered by questions about the truth/validity of cognitive hypotheses.

In the seventies, robotics passed through a flourishing period while designing technically sophisticated robots for quite pre-structured environments. However, transferring the robots into more 'real life' environments led to an incommensurable series of problems. The end of the eighties shows an offshoot in the robotics community, which is particularly marked by Brooks paper of 1986. Experimentalists acknowledged the limitations when robots have to deal with realistic environments, and concentrated on implementing low-level reactive systems. We denote this approach by *Sensory-based Robotics* (Design) after [Lyons *et al.*, 1989], or generally as "*behaviour oriented AI*" [Steels, 1994]. The new approach includes *motor-schema's* [Arkin, 1990], a notion originating from psychology. It refers to a pattern of "knowing-how" (to execute an action), and incorporates a (mental) motor-image [Decety, 1996] as well. In robotics, a motor-schema comprises certain activation patterns of the effectors and is triggered by sensor data. Moreover, the schema's performs rather autonomously: when triggered they invariably result into an action.

Sensor data arrive as a flow of values. Human beings (and robots designers as well) seem to have inherited perception mechanisms which emphasise patterns and disguise many irregularities. So, *artificial* perception is rather non-intuitive for human observers. They are easily led to misinterpretations, when they discuss other types of cognitive creatures. Hence, it makes sense to explicitly distinguish between *frames of reference*, for instance, that of the designer and that of his robot. We introduce the notion of *cognitive* basis, which helps to distinguish frames of reference in a discussion of cognition and intentionality. Moreover, using this notion, one can compare how different (types of) creatures are "carving up the world" through their sensors.

Present day technology challenges many qualitative theories of cognition by providing working mechanisms, robots, computers etc.. Indeed, one is led to the conclusion that *action* and *acting* are among the concepts deeply related to cognition.

In section 2, the notion of cognitive basis is introduced, and illustrated by means of an ultra sonic sensor. In section 3, we discuss perception problems, i.e., the interpretation of the sensor data. We focus on actions as an element of cognition in section 4. We connect the notion of intentionality with performing a motor schema. Finally, we attempt to define more formally what we like to call a *motor-schema (or motor-image) basis*. The result and novelty of our treatment is that (potential) actions are included into the notion of cognition.

2 Cognitive basis

2.1 Robot design

A robot consists of *effectors* or *actuators, sensors* and - what we metaphorically call - the *wiring* between them. The actuators are the foundation of any robotic design, because they determine (and constrain) what the robot might do, i.e. they circumscribe its 'raison d'etre'.

Our discussion stays mostly at the conceptual (logical) level so that we really address a *logical actuator*, which is any combination of (mechanical) hardware and software that can transform the state of the robot and its environment. Similarly, for sensors we introduce *logical sensors:* any combination of hardware and software which measures the state of the system and the environment [Henderson, 1990]. The actuators and the sensors are connected through a wiring consisting of the logical (or influential) connections between them. At an elementary level a simple wiring might do. The more sophisticated the aims of the designer, the more complex these "*wirings*" might be so that one may even speak of an "intelligent'' wiring. Intelligent, not because the wiring itself is that smart, but because the designer looked for "smart" connections. Our analysis addresses the realisation of these connections.

A motor-schema involves sensors, wiring and actuators and is a building block for (the design of) a robot. It consists of rather simple perceptual and motor activities. Each motor-schema has its own dedicated sensors. A *logical sensor* suits a motor-schema if it enables discrimination of the situations for which the schema has to become active. Complex actions may be orchestrated with the help of several motor-schema's. A complex situation is thus decomposed in line with the specific observations allowed by different sensors.

2.2 Definition

We introduce the notion of "*sensor basis*" analogous to the notion of "knowledge basis" in [Rauszer, 1992]. For convenience in explaining the definition we use the term "knowledge", at the end of this section we redefine the term. Suppose an agent r, has at its disposal a set of logical sensors which measure certain attributes $\alpha \in A_r$. The sensors can assign an attribute α with a value $v \in V_\alpha$ to an object o in the universe of discourse U.

(i) $\alpha: U \rightarrow V_\alpha$, $\alpha(o) = v$; $\alpha \in A_r$; $v \in V_\alpha$; $o \in U$;

An attribute need not discriminate between any two objects, which is expressed by $\alpha(x) = \alpha(y)$. Rauszer defines an *indiscernibility* relation for agent r, as:

(ii) $\mathrm{ind}(A_r) = \cap\, \mathrm{ind}(\{\alpha\}) = \{(x,y) \in U\mathrm{x}U : \forall \alpha \in A_r, \alpha(x) = \alpha(y)\}$

$\mathrm{Ind}(A_r)$ is an equivalence relation and the set of equivalence classes is a partitioning of the universe U. Thus, if two objects fall within the same equivalence class $[o]_{Ar}$, it means that the agent cannot distinguish one from another. The set of all equivalence classes :

(iii) $E = \{ [o_1]_{Ar} \ldots [o_n]_{Ar} \ldots\}$

is called *the knowledge basis of an agent* over the universe of discourse U, determined by its set of attributes A_r as handled by its set of logical sensors. The knowledge basis indicates which objects can *actually* be distinguished by the agent. Hence, it provides the base for any knowledge the agent *can* have about its environment. We discuss some further notions illustrating the useability:

The *positive* knowledge of r *about* set X consists of the set of equivalence classes generated by the elements of X:

(iv) $I^r(X) = \bigcup_{o \in X} [o]_{Ar}$;

X is *positively known* by r, if the positive knowledge $I^r(X) = X$. This means that r can (positively) distinguish each element of X from all other elements of X.

The *negative* knowledge $I^r(X^-)$ consists of the objects in X^- (X's complement) of which r can determine that they are *not* in X. The *knowledge of r about* X, $K^r(X) = I^r(X) \cup I^r(X^-)$; the knowledge of r about X is *complete knowledge* if $K^r(X) = U$;

The idea of positive knowledge is the most relevant for our purposes. We (as designers) can describe the environment of a robot as consisting of a set X of objects, but the positive knowledge of a robot indicates which of these objects it can (possibly) observe. One has to be careful in concluding that the environment is *positively known* by the robot: sensors do not always discriminate objects as we would like them to do, a topic which is discussed in the next section.

In a robot design different components are brought together. Above, we distinguished *sensors* from the *wiring*; consequently the above definitions apply twice. That is, call S the set of attributes for which the logical sensors produce values, then ind(S) is the *sensor basis* E_{sens} of the agent (an example is given below). We retain the title *knowledge* basis while applying the definition *to the wiring*. Calling C the set of logical connections or "information processing functions" implemented in the wiring, then ind(C) is the *knowledge basis* E_{know}. Any robot comprises both bases.

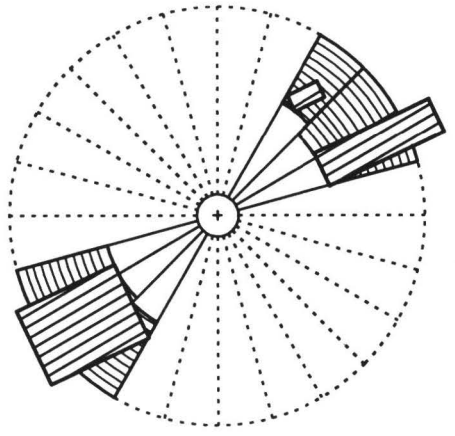

Figure 1, an ultrasonic sensor image

Example: In [Bomhof *et al.*, 1992] a mobile robot with an ultrasonic (US) sensor is described. The sensor readings are an angle under which the object is spotted, and a distance. The sensor basis E_{sens} consists of *cones* which either are occupied from a certain distance onwards or empty (see

Figure 1). Any information picked up in the environment represents a compound of such cones.

In the next subsection we treat the relationship between the sensor basis and the knowledge basis ending up in the definition of the cognitive basis.

2.3 Sensor and knowledge basis

The information flows from the sensor basis E_{sens} to the knowledge basis E_{know}. Hence, ideally E_{sens} and E_{know} *fit* to one another. As in information theory, one can determine how much information the sensors forward to the wiring. The basis is the number of states known to be possible at the source which is called *entropy* in information theory. The amount of information forwarded is, moreover, bounded by how many of these possibilities can be excluded at the end of the channel. The source is the sensor basis E_{sens}, the end of the channel is E_{know}. For proper processing E_{know} needs to respect relationships existing in E_{sens}; e.g., if the sensor basis is as in

Figure 1, adjacent cones of E_{sens} need to be treated as adjacent in E_{know}. Formally, this is expressed by requiring that E_{sens} maps by a homomorphism[1] to E_{know}. If, by mistake, there is no proper mapping, no real information can be exchanged.. Moreover, if E_{sens} can be mapped onto E_{know} (the mapping is a surjection) the sensory system provides the maximum of information which the wiring E_{know} is able to process and we say that the sensor basis is *suitable* to the knowledge basis. The other way around, if E_{know} can be mapped onto E_{sens} the wiring can process the maximum of the information originating from the sensors.

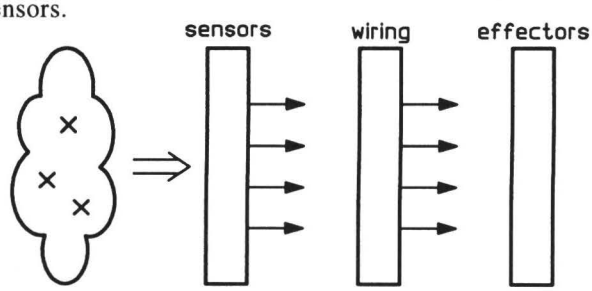

Figure 2, sensors, wiring and effectors

The aim now is to define an *internal cognitive structure* for a robot, denoted by Φ. It should consist of those (classes) of objects $o \in U$ that can be distinguished by the sensory system as well as by the wiring. The sensors and the wiring (sensor and knowledge bases) must have "positive knowledge" (definition (iv)) about them. Technically we can define:

[1] A homomorphism is a mapping that retains the relationships among the elements. In a robot it is fixed by the implementation.

(v) the *cognitive basis* Φ: if τ is a homomorphism from E_{sens} to E_{know}, Φ consists of the equivalence classes induced by τ.

The definition says that Φ consists of just those elements of the sensor basis that can be processed by the wiring[2]. The sensors and the wiring together deliver the cognitive basis Φ.

3 Artificial perception

3.1 Sensors and Objects

In Figure 1, the US sensor does not discriminate the two situations and the robot cannot find the corridor. One might try to *refine* the angle readings by adding an infrared (IR) sensor. An IR sensor can emit fairly precisely directed light beams, as reading is based on the reflection of the light (measuring distances is more complicated with this technique, and we will not consider it). On the face of it such a sensor might be used to increment the angle measurements. The aim is to extend the cognitive basis Φ; but such an extension is not straightforward at all. The behaviour of a light beam is quite different from a sound beam. Whereas cloth reflects a sound beam rather well, it can completely absorb light beams, and some objects are not detected at all by the IR sensor. Simply adding IR data (e.g., that no object is found) to the US data may cause inconsistency.

An elementary notion in *symbolic AI* is that of an (individual) object. This is true for most apparently suitable logical systems - such as [Rauszer 92] as well. Objects, however, pose a problem for artificial perception. The *existence* of individual objects has to be extracted from the sensor information. But this goes far beyond a simple interpretation of the sensor data. The sensors deliver only series of values of attributes, but from which objects the values originate is not detectable from the sensor signal itself. The idea of a perception basis was already given in [George, 1961]. His basis is indeed generated by simply joining the data of different sensors in extra dimensions. Still, this provides no answer as to how to "interpret" the sensor data.

In the definitions given above, the cognitive basis is constructed starting from external objects. The equivalence classes, are sets of attribute values observed when sensing a particular object. Within the cognitive basis the "objects" are but sets of observed properties, i.e., in advance of any cognitive activity the creature has to be "taught" about the objects. The designer has to determine which attribute value combinations do indeed *count* as a certain object. In any case, for whatever approach, there remains an intriguing practical problem of determining which combination of attribute values belongs to the same "object". This is essentially the problem of *sensor data fusion*. Any theory of cognition will be plagued by the problem of object identification.

[2] τ induces an isomorphism (that is a one-to-one homomorphism) between the sensor basis and (a part of) the knowledge basis.

3.2 The frame of reference

To recognise an object, the robot designer has to teach his robot. Here, frames-of-reference are interwoven. A robot is guided by its internal processing. Inputs from the sensors change the internal state of the creature. Call the set of *possible internal states* of the creature N. A certain sensor input makes the internal state $v_0 \in N$ of the creature change into $v_1 \in N$. We use the cognitive basis to assign a meaning to this processing. The cognitive basis is stated in antropomorphic terms, the symbols in the cognitive basis are (representational) shorthands for human (designer's) statements about the world. The question is whether it is really legitimate to ascribe a cognitive state to the creature. [Rosenschein, 1985] in developing his theory of *situated automata*, gives the following definition:

(iv) agent x is said to know a proposition (φ) in a situation where its internal state is v if (φ) holds in all possible situations in which x is in state (v).

We will not discuss whether in (iv) the term "know" is the most ideal. Our interest is in whether (iv) captures a useful cognitive notion. Let's first note that the definition covers unintended cases. E.g., consider a tree trunk: *"if a tree trunk has 78 rings then it indicates that the tree is 78 years old"* [Stalnaker, 1984]. The tree trunk satisfies (iv), but we are reluctant to ascribe a cognitive state to it!

Definition (iv) has a more serious defect in that it does not lay down any causal or process-like relationship between v and φ. The consequence is that, if agent x is in state v but φ doesn't hold, the conclusion can only be that the observer made a mistake while interpreting v. In fact, the relationship between v and proposition φ is not (much) more than that between the tree trunk and the proposition that *"the tree is 78 years old"*. Taking this route, one can, in a certain sense ascribe as much cognition to a creature as one likes, but it does not clarify the cognitive state of the creature. (We are in a certain sense commentating our own state of mind).

4 Actions

4.1 Intentionality

Above we were going through perception and ended up observing that definition (iv) is too liberal to delineate a creature's inherent cognition. The essence and the intriguing aspect of robot design is that ultimately *some* actions must result. Concerning robotics [Arkin, 1990] notes: *"perception is meaningless without the context of motor action"*. We need to change the perspective a little: we observe a robot which is *acting* and try to capture patterns of actions that are obviously aimed at bringing about certain results. This "purposeful" bringing about of changes in the environment is often called *"intentionality"*.

Example: As an illustration we consider a robot provided with an obstacle avoidance procedure and a goal finding procedure. It interprets the sensor data of figure 1 as an *artificial potential field*. Occupied cones are considered as a source of resistance, while the goal (given by co-ordinates in the same map) is taken as an attractive source. The magnitude of these forces decreases with increasing distances. (To visualise it one often represents the potential field as a landscape in which the repulsive sources form mountains and the attractive sources are valleys.) The robot steers itself along a route of low resistance, i.e. through valleys in the landscape. This and similar procedures work rather well in implementing obstacle avoidance [Khatib, 1986][Penders *et al.*, 1994].

We might infer that the robot has the *intention* to avoid obstacles, but the avoidance of obstacles is not directly implemented. There is *no* point in the internal processing, where it is concluded "this is an obstacle", so "avoid it". Within the cognitive basis Φ we cannot draw this conclusion, since, as seen already, the sensor readings do not allow for it. The potential field procedure is a "trick" implemented to obtain this result[3].

For convenience, we identify a motor-schema with the internal state v which it tends to bring about. For the robot using the obstacle avoidance motor-schema (implemented with the potential field procedure), v is an "equilibrium" state, from which no (new) impulses will reach the actuators. The performance of the robot is generalised in the following statement:

(vi) *performing motor-schema* v: in a situation where the sensor inputs do cause the mechanism to be in an internal state different from v, it performs until its same sensors cause v to occur.

Definition (vi) describes a causal process. Moreover, it refers only to internal features of the creature, the definition is directed inwards the creature. However, performing a motor-schema does change the environment, something that is not explicitly mentioned in (vi).

As external observers (and robot designers) we want to express what happens in the environment within our frame of reference. We ascribe an *intention* to the motor-schema.

(vii) A motor schema v is said to be an implementation of *intention* γ if in a situation where γ is not (yet) the case, motor-schema v is triggered and (under normal conditions) motor schema v brings about a situation in which γ holds.

The robot with the potential field procedure avoids obstacles rather successfully, though "obstacle avoidance" is defined only in our frame of reference. We, external observers, ascribe the attitude to the creature, and assign a sense γ to the motor schema v.

We required in (vi) that a motor-schema performs until a state v occurs. v should be caused by sensor inputs of the same type as that which caused $\neg v$. Thus a motor-schema must have an *end* definable in terms of its sensor inputs. The internal state v, which characterises the motor-

[3] The idea of an artificial potential field procedure is derived from physics, where its implications are rather different.

schema, must correspond to some (for the creature itself observable) feature of the future state of the environment. If this requirement is dropped we can have, for instance, a robot which releases a balloon whenever its sensor detects something. The robot has no feedback on its own actions (that is on releasing the balloon), or more precisely, it has no feedback of the type which originally forced it to perform. Such a robot seems rather close to the tree trunk above, which indicates the age of the tree.

In robotics, it is straightforward to question: "What is the sense of collecting information, if it isn't used in action?" A robot isn't but an acting device! For living species one might ask a similar question, separating perception from action and setting perception apart as an independent phenomenon.

4.2 Motor-image

Sensory-based robotics uses motor-schema's as the primitive building blocks with which an architecture of a robot is set up. A motor-schema in robotics is the analogon of the psychological concept of a motor-process (called motor-schema as well). In psychology it denotes the complex mechanism which links senses to the central nervous system and the effectors. The motor processes (incorporated in the schema) result in the execution of an action. Motor-schema's work like cybernetic loops or servomechanisms [Berthoz, 1996].

The dual of a motor-process is a *motor image*. "*Motor imagery can be defined as a dynamic state during which a subject mentally simulates a given action*"[Decety, 1996]. A motor image implies a subject feeling himself performing an action, and imagined and executed actions share central bodily structures. The motor image is the "symbolic" content of the imagery [Annett, 1996]. Motor imagery is said to comprise the activation of an action plan. The motor image, though based on the sense and motor data, is an *abstraction* from these data. Motor-schema's provide the foundation for the motor image.

Example: At the age of 4, my son was speaking to his friend (slightly older) about stairs. We were living at the second floor, our stairs were straight and very steep. The friend said "you have a long stair-case" pointing with his arm sloping upwards. My son agreed. The friend lived at the fourth floor, and their staircase rose in a spiral of eight separated staircases connected by landings. "Our stairs are like this .. ", the boy said, spiralling down with his finger and extending the movements with his arm and body. "Yes", my son shouted: "like this..." , starting a great turning movement and while doing so, he whirled downwards, laughing.

A flight of stairs is an example of a concept consisting of motor-images; it is hard to define what a flight of stairs is without referring to bodily movements. The boys show the connection of motor-images with motor-schema's.

4.3 Motor-schema basis

We noticed earlier the difficulty of identifying objects. For analysing a *robotic* design the cognitive basis as defined, seems sufficient because the robot designer provides the necessary frame-of-reference. However, when discussing *natural* (human) beings no external frame-of-reference is available, and the ability to perceive distinct objects needs to be founded somewhere within the being. The importance of motor imagery in cognition suggests that motor imagery needs to be incorporated within the definition of the cognitive basis. As a preliminary attempt we propose an extension to the definitions of cognitive basis above.

An agent r, has at its disposal a set A_r of input channels or logical sensors and a set of motor-schema's N_r. The sensors (input channels) $\alpha \in A_r$ assign one or more motor-schema's to an object o in the universe of discourse U.

$$\text{(ix)}\quad \alpha: U \rightarrow P(N_r),\ \alpha(o) = \{v: v \in N_r\}\ \ o \in U;$$

As before we can define an indiscernibility relation for a certain agent. In words, the definition will allude to: objects are distinguishable from one another only if they trigger one or more different motor-schema's.

$$\text{(x)}\quad \mathrm{ind}(A_r) = \cap\, \mathrm{ind}(\{\alpha\}) = \{(x,y) \in U \mathrm{x} U: \forall \alpha \in A_r,\ \alpha(x) = \alpha(y)\}$$

So, we can define a *motor-schema* or *motor-image basis* as the set of equivalence classes of objects which trigger different sets of motor schema's. Hence, if two objects fall within the same equivalence class $[o]_{Ar}$, it means that the agent (re-)acts similarly when observing them. The motor-schema or motor-image basis is the set of equivalence classes:

$$\text{(xi)}\quad M = \{\ [o_1]_{Ar} \ldots [o_n]_{Ar} \ldots\}$$

In (ix) the inputs are taken as mapping objects *directly into motor-schema's*. Each motor-schema incorporates (parts of) the perception and knowledge basis as previously defined. As in section 2 one may define mappings between the motor-schema basis and the perception, knowledge and cognitive basis. Roughly, what might be deleted of the latter bases are precisely those parts which *do not* trigger a motor schema.

We accent that definition (ix) is rather preliminary and may contain some (not yet foreseen) technical flaws. Besides this, we have to emphasise some more principle points. The definition starts from objects, but as we have seen, objects do not have a universal (cognitive) status shared among all cognitive creatures. Another principle point is that objects must have an intentional "significance" for the creature under consideration. By requiring that a motor-schema be triggered, a rather basic type of intentionality is implicitly incorporated in definition (ix).

For practical applications, it will be a problem to discriminate between different motor-schema's and in particular motor-images. However, we achieve with definition (xi) a demonstration of a way to incorporate actions as basic elements into the concept of cognition (and "intelligence"). Suppose an agent that can only perform motor-schema's (a robot for instance) and that misses the ability to form images. This agent cannot but act on ob-

serving an object. In fact, practitioners in, for instance, biology make reference to actions when they are comparing intelligence of one species with another one, there are no alternatives.

4.4 Interaction

Individuals of the same species share the same *types* of senses and the same *types* of motor-schema's (and motor-images). Thus, we have groups of agents that share much of their cognitive and motor-schema bases. In this case one can easily define a *common* cognitive and motor-schema basis. The definitions of cognitive basis and motor-schema basis are indexed by the agent r; by letting the index range over the group, the shared common bases are obtained. The *common cognitive* and *motor-schema* bases are the intersection of the individual bases. The shared bases allow to define interaction and communication. Recall that, according to information theory, the amount of information carried by a signal depends on how many alternatives the receiver knows to be possible at the source of the signal. Creatures of the same "species" with limited bases, have few possible interpretations for observations. Moreover, if they can only perform motor-schema's (no imagery) they quite straightforwardly interact with each other. Some define such interaction as low-level communication: *"A structural coupling between entities resulting in co-ordination of their actions necessary for their mutual viability"*(Maturana, cited in [Stewart, 1995]).

5 Conclusions

Approaching the cognition concept from the engineering (or design) perspective of robotics, we were advantageously enforced to be quite pragmatical. We introduced formal notions like sensor, knowledge, and cognitive bases. With them one is able to pinpoint one's frame of reference from which artificial cognitive creatures are viewed. Moreover, the whole issue of intentionality is clarified as belonging pre-dominantly to the frames of reference of the observer or designer. The *situation-action* perspective leads us to rethink the idea of a cognitive basis. The spectrum of (possible) actions becomes an integral part of a more encompassing idea of cognition. In this idea, motor-schema's (and possibly associated motor images) become just as important for the designer as they are for natural scientists studying *living* nature. In a sense, AI has just begun to assess the importance of such notions for *artifically* living creatures.

References

[Annett, 1996] J. Annett, On knowing how to do things: a theory of motor imagery. *Cognitive Brain Research* 3 pp. 123-154; Elsevier (1996).

[Arkin, 1990] R.C. Arkin, Integrating Behavioral, Perceptual, and World Knowledge. *Reactive Navigation, Robotics and Autonomous Systems* 6, Elsevier Science Publishers B.V., 1990, pp. 105-122.

[Berthoz, 1996] A. Berthoz, The role of inhibition in the hierarchical gating of executed and imagined movements, *Cognitive Brain Research* 3 pp. 101-113; Elsevier (1996).

[Bomhof *et al.*, 1992] F.W. Bomhof and J.S.J.H. Penders, A Vehicle that uses Acoustic Radar for Collision Avoidance, *Proc. 25th ISATA Conference on Road Transport Informatics/Intelligent Vehicle Highway Systems* pp. 293-299, Florence, Italy, 1992, Publ. Automotive Automation Ltd, Croydon CR0 5 SB, England.

[Brooks, 1986] R.A. Brooks, A Robust Layered Control System for a Mobile Robot, *IEEE* 1986.

[Decety, 1996] J. Decety, Do imagined and executed actions share the same substrate?. *Cognitive Brain Research* 3 pp. 101-113; Elsevier (1996).

[George, 1961] F.H. George, *The Brain as a Computer.* Pergamon Press, Oxford 1961.

[Henderson, 1990] T.C. Henderson, Logical Behaviours. *Journal of Robotics Systems* 7(3), 1990.

[Khatib, 1986] Khatib, O., Real-Time Obstacle Avoidance for Manipulators and Mobile Robots. *International Journal of Robotics Research*, vol 5, 1986.

[Lyons *et al.*, 1989] D.M. Lyons, and M.A. Arbib, A Formal Model of Computation for Sensory Based Robotics. *IEEE Trans. on Robotics and Automation*, vol 5, No 3, june 1989.

[Penders, *et al.*, 1994] J.S.J.H. Penders, L. Alboul and P.J. Braspenning, The Interaction of congenial autonomous Robots: Obstacle avoidance using Artificial Potential fields. *Proceeding ECAI-94*, John Wiley & Sons, pp. 694-698, 1994.

[Rauszer, 1992] C.M. Rauszer, Knowledge representation systems for groups of Agents. *Proc. of Logic at work*, Amsterdam 1992.

[Rosenschein, 1985] S.J. Rosenschein, Formal Theories of knowledge in AI and Robotics, *New Generation Computing*, 3(4) 1985 pp. 345-357.

[Stalnaker, 1984] R. Stalnaker, *Inquiry*. Basil Blackwell, Oxford 1984.

[Steels, 1994] L. Steels, Equilibrium Analysis of Behavior Systems, in Cohn, Proc. ECAI 94, pp. 714-718.

[Stewart, 1995] J. Stewart, The implications for understanding high-level cognition of a grounding in elementary adaptive systems. *Robotics and Autonomous systems*, pp. 107-116 (1995)