Algorithm Portfolios Based on Cost-Sensitive Hierarchical Clustering

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Abstract

Different solution approaches for combinatorial problems often exhibit incomparable performance that depends on the concrete problem instance to be solved. Algorithm portfolios aim to combine the strengths of multiple algorithmic approaches by training a classifier that selects or schedules solvers dependent on the given instance. We devise a new classifier that selects solvers based on a cost-sensitive hierarchical clustering model. Experimental results on SAT and MaxSAT show that the new method outperforms the most effective portfolio builders to date.

1 Introduction

Algorithm portfolios are an essential tool for boosting problem solving performance. In essence, the idea of algorithm portfolios is to select one or schedule several solvers out of a pool of algorithms based on the problem instance that is to be solved. This technology has proven key for providing state-of-the-art performance in satisfiability (SAT), quantified Boolean formulae (QBFs), and constraint programming (CP) as exemplified by the performance of portfolios in the respective solver competitions.

1.1 Related Work on Algorithm Portfolios

Algorithm portfolios, at least in their most recent advent, were pioneered by Gomes and Selman [2001] and Xu *et al.* [2008]. The first really prominent instance of a solver portfolio was SATzilla 2007, a SAT solver portfolio. It was based on a linear regression model to predict log runtime for each solver. For a while, the trend was towards more sophisticated machine learning models, such as a hidden-class portfolio generator [Silverthorn and Miikkulainen, 2010] or collaborative expert portfolio management [Stern *et al.*, 2010]. In parallel, the idea to schedule solvers, meaning, to run a selection of solvers for some designated time, was introduced by Streeter and Smith [2007] and O'Mahony *et al.* [2008].

Based on these methods, Kadioglu *et al.* [2011] introduced the idea of scheduling solvers while still picking one long-running solver. The notable feature of this portfolio, named `3S`, was that it used a low-bias (the authors call it "non-model based") machine learning technique for selecting the long running solver. Namely, the latter is conducted by means of a k-nearest neighbor approach which proved very effective for SAT. The 2011 and 2012 incarnations of SATzilla [Xu *et al.*, 2012a; 2012b] followed this trend and introduced a cost-sensitive, low-bias classification model approach based on random forests and voting. A recent comparison of the `SATzilla-2012` and the `3S` portfolio building approaches was conducted by Amadini *et al.* [2013] for building a portfolio of CP solvers which revealed a statistical tie between both methods for this benchmark, whereby `3S` appears to be performing marginally better.

1.2 Motivation and Scope

The motivation of this work is to provide a portfolio builder that works efficiently across a wide range of problem domains. For SAT and for CP we have fairly well-established feature sets that can be used to characterize a given problem instance and predict which solver(s) will be most effective at solving it quickly. However, we strongly believe that algorithm portfolios could be equally effective in boosting solver performance in other domains, such as MaxSAT or global continuous optimization or mixed-integer programming (MIP) where no good feature sets are readily available.

We expect that the `SATzilla-2012` methodology will generalize to other domains better than `3S` as each feature that has little predictive power regarding which solver is better suited for solving a problem deteriorates k-nearest neighbor-based `3S` performance. While there are ways to handle this (e.g., feature selection [Guyon and Elisseeff, 2003]), it is at the very least tedious for the non-expert to have to select the right features. Moreover, even when using scaling techniques, k-nearest neighbor cannot give different weight to features in different parts of the feature space. `SATzilla-2012` on the other hand can easily accommodate features which are not helpful and use features only in those areas of the search space where they actually help us differentiate between solvers.

On the other hand, `3S`'s scheduler is based on traditional optimization MIP technology while `SATzilla-2012` uses a heuristics-based presolver schedule. Surprisingly, we found that training this presolver takes a significant amount of time in `SATzilla-2012`. Furthermore, `SATzilla-2012` trains one random forest for each pair of solvers. This creates a computational bottleneck as the training time obviously

squares when the number of solvers doubles. One goal of this paper is to perform cost-sensitive multi-class classification directly and not by means of binary classification in order to alleviate this computational burden.

We propose a new portfolio builder that combines 3S's static scheduler with a new algorithm selector based on cost-sensitive hierarchical clustering (CSHC) which creates a multi-class classification model, runs orders of magnitude faster than SATzilla-2012, and is less sensitive to poor feature sets than 3S. We describe the method in detail and provide extensive empirical results comparing CSHC with SATzilla-2012 and 3S on various benchmark sets for portfolio generators.

2 Toward A New Algorithm Portfolio Builder

Clustering is a standard technique in unsupervised learning, equally fundamental and simple as k-nearest-neighbor classification in supervised learning. The two methods bear methodological similarities as well. The result of k-nearest neighbor learning is the labeling of compact areas of the feature space by one class, just as clustering groups of instances into compact clusters. In fact, the k-nearest-neighbor in 3Swas inspired by cluster-based instance-specific algorithm configuration shown by Kadioglu *et al.* [2010].

While clustering is certainly appealing, it makes sense to center clusters at the test instance that needs to be solved. That is exactly what the k-NN approach does. Moreover, traditional clustering is unsupervised. For the purpose of algorithm portfolios, we would like to group training instances in such a way that they can agree on the class they should be labeled with. For us that means that training instances in the same cluster should preferably not disagree violently on which solver solves them most efficiently (or at all, in case of timeouts). Finally, while clustering is traditionally based on some metric of distance, to accommodate poor feature sets we need a clustering method that allows us to select when or under what circumstances we use the dimensions that features provide are used for determining what goes into the same cluster.

2.1 Cost-Sensitive Hierarchical Clustering

We propose a learning method which we named *cost-sensitive hierarchical clustering (CSHC)*. High-level, the method proceeds as follows. First, all instances are in the same cluster. Now, for each cluster in the current set of clusters, we test whether a given minimum number of instances is still present in that cluster (we typically set this required minimum to ten instances). If not, we remove the cluster from consideration for further partitioning. Otherwise we split the cluster in such a way that the instances within each of the two clusters maximally agree on the class they should be labeled with.

We will investigate a variant where we add another phase, where we consider merging clusters again for which the split resulted in diminishing cross-validation performance.

At run-time, we compute the given instance's feature vector and determine which cluster it belongs to. Then, we employ the solver that performs best on the training instances in this cluster.

Cost-Sensitive Learning Problem

More formally, we consider the following (incomplete) classification problem. Given are a set of classes C and a set of training instances T, each associated with a feature vector $f \in \mathbb{R}^F$. Moreover, we are provided with a cost-vector that associates each instance $i \in T$ with a cost $m_{i,c} \geq 0$ which represents the cost of (mis-)classifying instance i by class $c \in C$. The task is to infer a classification algorithm which will assign a class to new instances such that their associated misclassification cost is minimized. We label this classification problem incomplete as we obviously do not know what the misclassification costs for the given instance are or how these can be inferred from the misclassification costs that we observe for the training instances.

It is worth noting that the problem considered is similar yet fundamentally different from semi-supervised problems considered in machine learning. In particular, Elkan [2001] considered the problem where the misclassification costs are determined by a given $|C| \times |C|$ matrix which assigns a misclassification cost to each pair of classes, where the first is the preferred class of the instance, and the second is the class we label it with. Obviously, when building an algorithm portfolio, there does not exist and, in any case, we would not have access to such a class-misclassification matrix.

It is interesting to note that the model-based portfolio approaches [Xu *et al.*, 2008; Silverthorn and Miikkulainen, 2010] essentially aim to predict the misclassification costs for a given instance. One advancement was the realization that better predictions are obtained when we focus on predicting a preferred class *without* taking the detour of forecasting the misclassification costs for each class for the given instance [O'Mahony *et al.*, 2008; Kadioglu *et al.*, 2011; Xu *et al.*, 2012b].

There exist many other cost-sensitive learning methods (see for example [Lenarcik and Piasta, 1998; Ting, 2002; Zadrozny *et al.*, 2003; Klinkenberg and Rüping, 2003; Geibel and Wysotzki, 2004; Wysotzki and Geibel, 2009]). It is beyond the scope of this paper to give a comprehensive overview. However, the only cost-sensitive multi-classification approaches for the cost-model that applies to portfolios that we are aware of are the ones employed by 3Sand SATzilla-2012, whereby the latter is based on a series of binary classifications.

Approach

During CSHC's learning phase we maintain a set of clusters, starting with all training instances in one cluster. In each iteration, we remove one cluster from the current set. If it is too small, we do not partition it further. Otherwise, we partition the cluster in two parts by running a hyperplane through the feature space so that instances fall on either side of the plane.

When labeling an instance i with class C we incur the cost $m(i, C)$. The total (mis)classification cost when labeling a subcluster with a specific class is the sum of all costs for all instances in that cluster. The cost of a binary split is the cost of labeling each subcluster with a class that gives the lowest cost. We select a hyperplane to split the cluster so that the cost of the binary split is minimized. If none of the sub-clusters are empty, we add both to the current set of clusters.

In a potentially following phase, we consider undoing some cluster splits based on the cross-validation performance that we would achieve by labeling the whole cluster with one class, compared to the cross-validation performance when doing the same for the two sub-clusters. If the performance of the split is not better, we undo the partition.

At runtime, for the first 10% of available time, the portfolio executes the same static schedule as `3S`. If this does not result in a solution, we use the hyperplanes used for splitting the base set to determine which cluster the test instance belongs to, and we try solving it with the solver that has the overall best performance on all training instances in that cluster.

Decision Trees

As we will discuss shortly, in practice we will consider axis-parallel hyperplanes to obtain a tractable training method. This means that the clustering approach could very well also be viewed as a decision tree approach where the ground set of training instances is repeatedly partitioned by branching on individual features. The main difference to existing cost-sensitive desision tree methods is the way how we compute the cost of a split. Instead of considering entropy or cost-sensitive entropy, we favor splits where, in both parts, the instances can agree on a consensus label that may not be perfect for any one instance but that incurs minor costs for all.

2.2 Bagging, Maximum-Margin Hyperplanes, Feature Augmentation

In this section, we discuss several alternative techniques that we considered adding to the basic CSHC methodology. Later we will test these empirically and quantify their effect on overall portfolio performance.

Bagging

The first technique we consider is bootstrap aggregating (bagging), a well-known technique in machine learning for improving the stability of classification and regression algorithms. In our case, we generate bootstrap samples to create training sets which are then clustered. That is, rather than creating just one clustering using all training instances, we create multiple clusterings based on subsets of the training set.

The obvious question arises how we should then combine the potentially conflicting classifications from different clusterings. We propose four different ways on how this information can be combined:

- **PAR-10 Aggregation:** Collect, for each clustering, the respective training instances in each cluster that the test instance belongs to. We can assemble these instances into a set or a multi-set of instances. Then, to determine the solver the given instance should be solved with, we compute which solver has the best performance in terms of average runtime with timeouts penalized by a factor of 10 (PAR-10) on the set or multi-set of instances in the various different clusters the test instance belongs to.
- **Winner Aggregation:** Determine the best class for each cluster the test instance belongs to. Then we label the test instance with the class that was chosen most often.
- **Rank Aggregation:** Rank the classes in each cluster the test instance belongs to. Then, we choose the class that has the best average rank over all clusterings.
- **SATzilla-style Aggregation:** Recall that `SATzilla-2012` builds a random forest for each pair of classes (which, in our case, correspond to solvers). Using the analogy of axis-parallel clustering and decision trees discussed above (the only difference being how we split), each random tree can be viewed as a "clustering" of training instances. In `SATzilla-2012` the information from each "cluster" are aggregated by first aggregating over all trees, and then counting how many other solvers each solver is able to outperform. We can emulate this aggregation scheme by computing, for each ordered pair of solvers, for how many of our bagged clusterings the first solver outperforms the second. If this number is at least half, we say the first solver outperforms the second, otherwise we say the second outperforms the first. We then compute, for each solver, how many other solvers it outperforms. We choose the solver that outperforms the most other solvers.

Maximum-Margin Hyperplanes

Earlier, we said that we would compute a hyperplane to split the base instances such that the performance of the best solver on each side is maximized. This is, in general, a hard optimization problem. We consider two heuristics for computing such hyperplanes. The first is to consider feature-axis-parallel hyperplanes only which renders the resulting optimization problem tractable. Using this method, our clustering approach can be viewed as a decision-tree procedure. In a second variant, we consider accepting the best split according to an axis-parallel hyperplane, but then tilt it so as to achieve a splitting hyperplane that achieves the same base partition with a maximum margin. We found that non-axis-parallel hyperplanes do not boost performance, yet increase the learning time considerably, which is why we do not pursue this avenue further in this paper.

Feature-Augmentation

One welcome advantage that `CSHC` shares with the `SATzilla-2012` approach is the ability to accommodate features that have limited prediction potential. That is, we can add a bunch of new features or combinations of the existing features without fearing that performance would decline. We consider adding products and quotients of pairs of features to our feature set.

3 Analyzing the Components of `CSHC`

A priori it is not clear which of the variants of `CSHC` performs best. In this section, we therefore perform an experimental comparison of different versions of the cost-sensitive clustering approach we have proposed.

Typically, in the literature on algorithm portfolios we find that different papers consider different sets of features, differing sets of solvers, and differing train and test sets. Recently, Malitsky [2013] created an actual benchmark for algorithm

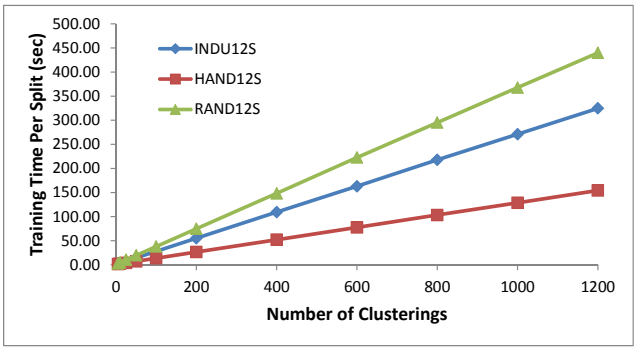

Figure 1: Training time of CSHC as a function of the number of clusterings

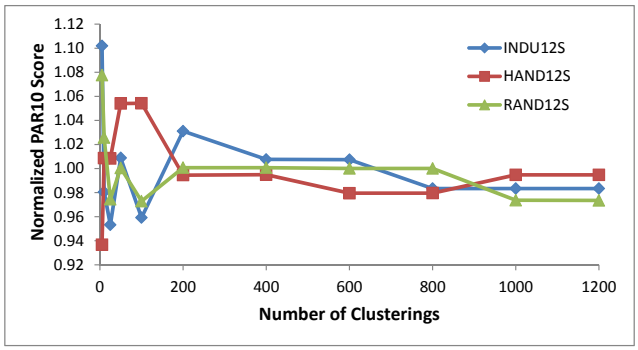

Figure 2: PAR-10 performance of CSHC as a function of the number of clusterings

portfolios that standardizes these choices. It allows us to compare different algorithm portfolio methods on a level playing field as the benchmark for a portfolio builder really consists of all, available features, the set of base solvers, as well as training and test sets.

All experiments in this section are based on the dataset provided by the UBC group[1] after SATzilla won the SAT Challenge 2012. The data is broken down into crafted, industrial, and random categories. Instances in each category were solved by the same 31 SAT solvers with a 1,200 second timeout. Malitsky [2013] removed all instances that cannot be solved by any solver within the allotted timeout and broke down each of the data sets into 10 parts suitable for cross-fold validation. Instances are characterized by the 125 features the UBC team proposed (option -base). For each of the three benchmark sets, we created five benchmarks with two, three, four, twelve, and all 31 solvers by removing solvers from the base set.

In the rest of this section, we evaluate the contribution of various components of CSHC to its performance and use the findings to tune basic choices in CSHC (how many clusterings to use, what aggregation mechanism to use, etc.). In Section 4 we then compare the resulting tuned CSHC with other portfolio solvers. To keep this latter comparison fair, we tune the components of CSHC on a different benchmark than the benchmarks we will use later to compare with other portfolio builders.

3.1 Number of Bootstrap Samples

First, we investigate the impact of the number of clusterings on the robustness, stability, and scalability of CSHC. We ran CSHC with various numbers of bootstrap samples ranging from 5 to 1,200, whereby each sample contains 60% of all available training instances. We also tested various other percentages but that had little effect on the overall trend. The experiments were run on the benchmark data mentioned above and results reported are the averages over the 10 data splits used for cross-validation.

Figure 1 shows, for each number of clusterings on the horizontal axis, the average training time per split on the vertical axis. There is one curve each for the industrial, crafted, and random instance benchmarks. As expected, we see that the training time of CSHC scales linearly as the number of clusterings grows. Training never took more than 7 minutes[2] per split on this benchmark even with 1,200 clusterings. This is massively faster than SATzilla-2012[3] which, on these benchmark sets with 31 solvers, needs CPU-days to be trained.

Figure 2 shows, again as a function of the number of clusterings, the normalized average PAR-10 score observed across the 10 splits. For each of the industrial, crafted, and random benchmark sets, the PAR-10 score plotted here is normalized by the average of the PAR-10 scores across all 10 splits. Note that, as the number of clusterings grows, this measure will eventually converge to 1, independent of the benchmark. We observe that CSHC is rather unstable for up to about 100 clusterings but begins to show reasonable stability after a few hundred clusterings.

While using more clusterings makes performance more robust, there is clearly a tradeoff with growing training time. For the rest of the experiments reported in this paper, we chose to use 800 clusterings which kept CSHC reasonably fast yet stable.

3.2 Aggregation

We discussed four different aggregation schemes earlier, PAR-10, winner, rank, and SATzilla-inspired aggregation. In Table 1 we present our numerical results when using these aggregators.

Our first observation from this data is that the SATzilla-inspired aggregation method is clearly inferior to all other techniques. Note that, while the method is inspired by SATzilla-2012, this does *not* mean that, within that portfolio builder, the aggregation method used is sub-optimal. First, SATzilla-2012 builds a different random forest for each pair of solvers. CSHC on the other hand builds just one set of clusterings which performs multi-class classification. The latter gives an advantage in terms of the time needed for learning. However, it may very well have an adverse effect on this

[1] http://www.cs.ubc.ca/labs/beta/Projects/SATzilla

[2] These experiments were conducted on a 4-core Intel Xeon 2.4 GHz machine with 24 GB RAM running Scientific Linux 6.1.

[3] Downloaded from http://www.cs.ubc.ca/labs/beta/Projects/SATzilla.

Table 1: Performance comparison of the four different aggregators with a timeout of 1,200 seconds. Shown is the average percent solved over the ten-fold cross validation.

SAT Family	PAR-10	Winner	Rank	SATzilla
Crafted	89.3	91.0	89.2	81.0
Industrial	96.4	96.6	97.2	87.2
Random	97.1	97.0	97.1	92.9

Table 2: Performance comparison of the three different aggregators using 2, 3, 4, and 16 solvers from the SATzilla 2012 benchmark (Timeout of 1,200 seconds). Shown is the average percent solved over the ten-fold cross validation.

SAT Family	#Solvers	PAR-10	Winner	Rank
Industrial	2	97.6	97.6	98.5
	3	97.1	97.8	98.1
	4	97.6	97.8	97.8
	12	96.5	96.9	96.8
Crafted	2	94.4	94.4	94.4
	3	94.1	95.2	95.6
	4	92.9	92.9	93.3
	12	90.8	92.7	90.8
Random	2	98.2	97.9	98.0
	3	96.8	96.3	96.5
	4	96.4	96.5	96.3
	12	98.3	97.9	98.2

aggregation method. Second, the way how we cluster the different bootstrap samples differs fundamentally from the cost-sensitive random-forests that `SATzilla-2012` creates.

Between the remaining aggregators, there is no clear winner. We therefore created more benchmarks by selecting subsets of base-solvers. Table 2 shows the comparison between the remaining aggregators on these additional benchmarks. Overall, we find that the rank-based aggregation performs with good average performance while displaying the smallest variance in performance. It works second best on the crafted and random categories and, across the board, best on industrial instances.

3.3 Combination Features

As discussed earlier, unlike `3S`, both `CSHC` and `SATzilla-2012` can naturally accommodate more features and simply not use them if they are not helpful. Given k original features, we consider adding k' randomly chosen pairwise products and quotients of these features to `CSHC`. If $f2 = 0$, the quotient $f1/f2$ is treated as 1 if $f1$ is also 0, and as a cutoff value of $\text{sign}(f1) \times 10^{36}$ otherwise.

Table 3: Impact of adding additional features based on quotients and products on the different SATzilla benchmarks with a timeout of 1,200 seconds. Shown are the average PAR-10 scores across the splits and the corresponding training time per split in minutes.

#Features added	Industrial		Crafted		Random	
	PAR10	TrTime	PAR10	TrTime	PAR10	TrTime
0	494	3.8	1402	1.9	419	5.5
25	519	12.3	1423	6.8	419	24.9
50	507	23.5	1423	12.6	419	47.2
100	505	69.8	1316	30.3	397	119
150	493	135	1380	61.4	408	210
200	482	237	1426	123	420	300

Table 4: Performance comparison of `CSHC` with and without merging on the SATzilla 2012 benchmark with a timeout of 1,200 seconds. Shown are the average percentage solved and the average PAR-10 runtime in seconds on the test sets of the ten-fold cross validation.

	`CSHC`+Merging		`CSHC`	
Benchmark	%	PAR-10	%	PAR-10
Industrial	96.7	548	97.2	494
Crafted	88.9	1445	89.2	1423
Random	97.0	432	97.1	420

Table 3 shows the result of adding $k' = 0, 25, 50, 100, 150,$ and 200 such feature combinations. For each benchmark we report the resulting performance in terms of PAR-10 score averaged over the 10 splits, along with the average training time needed per split. We find that adding products and quotients does not lead to a substantial difference in the PAR-10 performance on this dataset, at least on the industrial instances. On crafted and random instances, using $k' = 100$ results in a somewhat improved performance. However, the improvement is unstable across different benchmark categories and comes at the cost of 30 minutes to nearly 2 hours of training time per split, compared to under 6 minutes without these additional features. We therefore chose not to use such augmented features for the remainder of this empirical study.

3.4 Cross-Validation-Based Merging of Clusters

When describing the `CSHC` approach we discussed the possibility of undoing cluster splits based on a cross-validation. We implemented this technique and compare it to the plain cost-sensitive hierarchical clustering we proposed.

We show our results in Table 4. Across the board we observe that the merging of split clusters actually diminishes performance. We tested a number of other techniques for undoing splits, such as merging if the performance of the split declines on the instances left out for training by the current bootstrap sample. However, all these techniques showed the same trend: The simpler technique of cost-sensitive hierarchical clustering without cluster-merging performs better. This observation matches the well-known fact that, when constructing decision forests, it is better not to prune the trees.

4 Comparison with `SATzilla-2012` and `3S`

There are two portfolios which excelled in the last two SAT Competition/Challenges. In 2011, `3S` [Kadioglu *et al.*, 2011] won the crafted and random categories. In 2012, `SATzilla-2012` [Xu *et al.*, 2012a] won the industrial and crafted categories.

[Amadini *et al.*, 2013] compared the two approaches when building portfolios of constraint programming solvers. It was already noted there that `SATzilla-2012` needed much more time for learning, especially as the number of solvers increases. In terms of test performance, Amadini *et al.* [2013]

Table 5: Performance comparison of 3S, SATzilla-2012, and CSHC on the MAXSAT benchmark. Shown are the average percent solved (timeout 1,800 seconds) and PAR-10.

	3S		SATzilla-2012		CSHC	
MaxSat	%	PAR-10	%	PAR-10	%	PAR-10
MS Crafted	99.4	224	99.3	228	99.4	256
PMS Crafted	95.3	1014	99.3	155	99.3	196
PMS Indu	96.4	728	98.1	412	98.3	391
WPMS Crafted	91.4	1683	95.0	948	97.0	609
WPMS Indu	100	132	96.6	718	98.3	421

Table 6: Performance Comparison of 3S, SATzilla-2012, and CSHC on the SATzilla 2012 benchmark with a timeout of 5000 seconds. Shown are the average percentage solved and the average PAR-10 runtime in seconds.

	3S		SATzilla-2012		CSHC	
Benchmark	%	PAR-10	%	PAR-10	%	PAR-10
Industrial	88.0	6638	92.1	4444	93.1	4093
Crafted	81.8	10453	89.5	5760	90.9	5169
Random	96.6	2004	98.2	1165	99.0	870

found that both builders result in almost the same performance, with a slight edge in favor of 3S which was not statistically significant. To the best of our knowledge, to date this is the only comparison of SATzilla-2012 and 3S on a level playing field where both builders use the same set of solvers, the same features, and the the same train/test splits.

4.1 MaxSAT

Using Malitsky's portfolio benchmark [Malitsky, 2013], we compare CSHC with 3S and SATzilla-2012. In Table 5 we compare CSHC with 3S and SATzilla-2012 on various MaxSAT benchmarks. All builders use the same set of base solvers and the same features that are provided for each instance. The numbers represent the average test performance over the same ten cross-validation splits that are part of the benchmark.

The benchmark consists of instances gathered from the various categories of the 2012 MaxSAT Evaluation. There are five benchmarks in total: crafted unweighted MaxSAT (MS), crafted and industrial partial MaxSAT (PMS), and crafted and industrial weighted partial MaxSAT (WPMS). These instances were run with a 1,800 second timeout with 10 to 14 MaxSAT solvers, depending on the benchmark. We use the ten cross-validation splits provided by [Malitsky, 2013].

For the features, the MaxSAT instance was converted into an equivalent instance where all the soft clauses are unit. This is achieved by reifying the soft clauses. Finally, the computation of the features is performed using the SATzilla feature-code on the hard clauses of the MaxSAT formula.

We observe that 3S's performance is rather erratic. At times it works really well, other times it works significantly worse than SATzilla-2012 and CSHC. It performs equally well as CSHC on crafted MaxSAT benchmarks, and it clearly outshines all other methods on weighted partial MaxSAT Industrial. On the other hand, it works much worse on all remaining benchmarks.

Comparing SATzilla-2012 and CSHC, we find that the latter performs on par on crafted partial MaxSAT and better on all other benchmarks. Especially on the two weighted MaxSAT benchmarks CSHC works notably better than SATzilla-2012.

4.2 SAT

Next we use the benchmark based on data from the SATzilla-2012 webpage. This data utilizes the dataset provided by the UBC group coupled with their SATzilla portfolio Matlab code.[4] The data is broken down into crafted, industrial, and random categories. Instances in each category were taken from the 2012 SAT Challenge and run on the solvers at that competition (15 for Crafted, 18 for Industrial, and 9 for Random). Timeout is 5,000 seconds. [Malitsky, 2013] again removed all instances that could not be solved by any solver within the allotted timeout and provided ten standardized cross-validation splits.

Consider Table 6. We observe the same trend as we had noted on the MaxSAT benchmarks. 3S behaves erratically: On the random category it performs almost as good as SATzilla-2012 and CSHC, but on the crafted and industrial instances it performs much worse.

We further note that the cost-sensitive clustering approach again outperforms SATzilla-2012 on every category. However, while these results are highly encouraging, the ten splits that were provided by [Malitsky, 2013] are not enough to confirm statistical significance.

5 Conclusion

We devised a cost-sensitive hierarchical clustering approach for building algorithm portfolios. We applied this method to benchmarks from MaxSAT and SAT. The empirical analysis showed that adding feature combinations can improve performance slightly, at the cost of increased training time, while merging cluster splits based on cross-validation lowers prediction accuracy. Moreover, we found that aggregating across multiple clusterings based on class rank works most robustly. We then compared the new approach with the most successful state-of-the-art algorithm portfolios, SATzilla-2012 and 3S. We found that 3S's performance is rather unpredictable: for some benchmarks it works really well, while for others it builds under-achieving portfolios. SATzilla-2012 works much more stable but is outperformed on all benchmarks we tested by cost-sensitive hierarchical clustering. Furthermore, training CSHC is much faster than SATzilla-2012, especially as the number of base solvers grows.

Acknowledgements

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[4] Downloaded from http://www.cs.ubc.ca/labs/beta/Projects/SATzilla.

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